

# IS INFRASTRUCTURE CAPITAL PRODUCTIVE? A DYNAMIC HETEROGENEOUS APPROACH.

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# Motivation

- How important is infrastructure capital for economic growth?
- Since the seminal work of Aschauer (1989), a lot of studies have been concerned with the effect of public capital on economic growth.
- Standard way to incorporate infrastructure capital in an economic model is to introduce public capital as an additional production factor in a production function.
- In particular, Canning (1999), Canning and Bennathan (2000) and Röller and Waverman (2001) among others, attempted to measure the aggregate output effect of different types of infrastructure capital.

## Why this paper?

- There are five major caveats in previous empirical literature:
  - ① Non-stationarity of aggregate output and infrastructure capital.
  - ② Problems of reverse causality.
  - ③ Potential heterogeneity across countries.
  - ④ Multidimensionality of infrastructure.
  - ⑤ Monetary measures of public capital might be misleading proxies of infrastructure.
- The paper's approach allows us to address these caveats:
  - ① We use a panel cointegration approach to deal with the non-stationarity of the variables.
  - ② We test that the single (and common) cointegrating relationship among the variables can be interpreted as a production function.
  - ③ We allow for short-run heterogeneity across countries, and we test the homogeneity in the long-run relationship.
  - ④ We consider the multidimensionality of infrastructure by using a synthetic PCA index of telecommunications, transport and power.
  - ⑤ We use physical measures of infrastructure.

# Data

- A balanced panel of 88 countries and 41 years (1960-2000)
- Output has been approximated by using the real GDP in 2000 PPP US dollars from PWT 6.2
- Physical capital: perpetual inventory method with investment from PWT 6.2 and initial stock from PWT 5.6
- Human capital from Barro and Lee (2000).
- Infrastructure capital:
  - Electricity Generating Capacity (EGC) in kilowatts from United Nations Energy Statistics
  - Number of telephone main lines (MLINES) from Canning (1998) and International Telecommunications Union.
  - Road length in kilometers (ROADS) from the International Road Federation World Road Statistics.
  - These three infrastructure assets are summarized into a synthetic index constructed through a principal-component procedure.

## Production Function Approach

- We consider a Cobb-Douglas production function such that:

$$y = \alpha k + \beta h + \gamma z$$

where  $y, k, h$  and  $z$  are respectively output, physical capital, human capital and infrastructure capital in logs per worker terms. (CRTS assumed)

- Infrastructure capital appears twice in the equation (as part of  $k$ , and separately as  $z$ ).
- Thus, letting  $\tilde{k}$  denote noninfrastructure physical capital:

$$k = (1 - \theta)\tilde{k} + \theta z$$
$$\frac{\partial y}{\partial z} = \alpha\theta + \gamma \quad \text{where } \theta = \frac{p_z Z}{p_z Z + p_{\tilde{k}} \tilde{K}}$$

- Hence, the parameter  $\gamma$  captures essentially the excess return on infrastructure relative to other capital. Note also that  $\theta$  is typically a small number so that the difference between  $\alpha\theta + \gamma$  and the 'naive' estimate  $\gamma$  should be fairly modest.

# Empirical Strategy

- We have a panel dataset of 88 countries ( $N$ ) and 41 years ( $T$ ).
- Our approach is based on recent panel time-series literature.
- Therefore, the production function may represent a long-run cointegrating relationship.
- Given the above, this research is based on three steps:
  - ① Test the non-stationarity of the variables. [\[Details\]](#)
  - ② Test whether there exist a common cointegrating relationship or not. [\[Details\]](#)
  - ③ If the variables are cointegrated, estimate consistently the long-run parameters and test for homogeneity.

# Unit Root and Cointegration Test Results

Table: Testing Results

<b>PANEL A: Panel Unit Root Test</b>	
Variable	Test Statistic
GDP	-6.20
Physical Capital	-7.08
Secondary Education	-1.77
Infrastructure	-3.35

  

<b>PANEL B: Panel LR-bar Test</b>	
Maximum rank	Test Statistic
0	9.03
1	0.85

  

<b>PANEL C: Panel PC-bar Test</b>	
Minimum rank	Test Statistic
1	1.21

5% critical value for the null hypothesis of unit root is 1.96 in all cases.

## Estimation Method

- If there is only one cointegrating relationship among the variables, we can use the PMG estimator proposed by Pesaran, Shin and Smith (1999) [\[Details\]](#)
- This ML estimator allows the intercepts, short-run coefficients, and error variances to differ freely across groups, but constrains the long-run coefficients to be the same:

$$\Delta Y_i = \phi_i (Y_{i,-1} - X_{i,-1}\theta) + W_i\kappa_i + \varepsilon_i \quad i = 1, 2, \dots, N$$

where  $x_{it} = (\text{physical capital}_{it}, \text{human capital}_{it}, \text{infrastructure}_{it})$

$Y_i = (y_{i1}, \dots, y_{iT})'$ ,

$W_i = (\Delta Y_{i,-1}, \dots, \Delta Y_{i,-p+1}, \Delta X_{i,-1}, \dots, \Delta X_{i,-p+1}, \iota)$  and

$\kappa_i = (\lambda_{i1}, \dots, \lambda_{i,p-1}, \delta'_{i1}, \dots, \delta'_{i,p-1}, \mu_i)'$ .

- Moreover, long-run homogeneity can be tested.

# Estimation Results

[Additional Results]

Table: Estimation Results

Max # of lags	2	2	2	1	4	2
Information criterion	SBC	AIC	Imposed	SBC	SBC	SBC
Common factors	Yes	Yes	Yes	Yes	Yes	No
<b>Physical Capital</b>	<b>0.34</b>	<b>0.33</b>	<b>0.36</b>	<b>0.35</b>	<b>0.34</b>	<b>0.41</b>
t-ratio	35.2	30.5	22.7	31.4	32.4	33.4
hausman p-value	0.54	0.95	0.43	0.78	0.44	0.52
<b>Secondary Education</b>	<b>0.10</b>	<b>0.12</b>	<b>0.10</b>	<b>0.12</b>	<b>0.11</b>	<b>0.12</b>
t-ratio	15.6	14.8	8.09	18.7	17.1	16.0
hausman p-value	0.24	0.19	0.21	0.19	0.20	0.64
<b>Infrastructure</b>	<b>0.08</b>	<b>0.07</b>	<b>0.10</b>	<b>0.08</b>	<b>0.08</b>	<b>-0.02</b>
t-ratio	7.45	6.73	6.58	8.33	8.77	-1.49
hausman p-value	0.21	0.18	0.16	0.40	0.88	0.40
joint hausman p-value	0.44	0.38	0.24	0.25	0.45	0.85
Average R <sup>2</sup>	0.36	0.40	0.48	0.28	0.42	0.35
Observations	3432	3432	3432	3520	3256	3432

## Concluding Remarks

- Output, physical capital and human capital represent a cointegrating relationship in all the 88 countries under analysis.
- Our estimates place the output elasticity of infrastructure in a range between 0.07 and 0.10.
- This result suggests that there is an excess return of infrastructure capital over that of non-infrastructure capital.
- On the other hand, tests of parameter homogeneity reveal little evidence that the output elasticity of infrastructure varies across countries.

## Testing for non-stationarity

- Im, Pesaran and Shin (2003) propose a test based on the "normalized" average of ADF statistics computed for each group in the panel.
- Given the ADF( $p_i$ ) regressions:

$$\Delta y_{it} = \alpha_i + \beta_i y_{i,t-1} + \sum_{j=1}^{p_i} \rho_{ij} \Delta y_{i,t-j} + \varepsilon_{it}, \quad i = 1, \dots, N, \quad t = 1, \dots, T$$

- The test is based on:
  - $H_0 : \beta_i = 0$  for all  $i$
  - $H_1 : \beta_i < 0 \quad i = 1, 2, \dots, N_1, \quad \beta_i = 0 \quad i = N_1 + 1, N_1 + 2, \dots, N.$
- The IPS test statistic is shown to converge in probability to a standard normal variate under the null.
- Monte Carlo simulations show that the IPS test performs reasonably well in finite samples. In particular, given the dimensions of our panel, we could expect to obtain high power. [\[Go Back\]](#)

## Testing for Cointegration

- In previous studies, cointegration among variables has been assumed but not tested.
- In this multivariate panel setting, three questions emerge:
  - 1 Are the series cointegrated?
  - 2 If so, how many cointegrating relationships are there?
  - 3 Is this number equal for all units in the panel?
- We follow a two step procedure that allow us to answer these three questions:
  - 1 LR-bar Test  $\Rightarrow$  It gives the maximum cointegration rank
  - 2 PC-bar Test  $\Rightarrow$  It gives the minimum cointegration rank.
- If they coincide, we conclude that there exists one common cointegration rank among all units. [\[Go Back\]](#)

## LR-bar Test (Step 1)

$$H_0 : \text{rank}(\Pi_i) = r_i \leq r \quad \text{for all } i = 1, \dots, N$$

$$H_1 : \text{rank}(\Pi_i) = p \quad \text{for all } i = 1, \dots, N$$

- The LR-bar statistic converges to a standard normal as  $N$  and  $T \rightarrow \infty$ :

$$\Upsilon_{LR}(r|p) = \frac{\sqrt{N}[N^{-1} \sum_{i=1}^N LR_{iT}(r|p) - E(Z_K)]}{\sqrt{\text{Var}(Z_K)}} \Rightarrow N(0, 1)$$

where  $LR_{iT}(r|p)$  is the individual trace statistic for unit  $i$  and  $E(Z_K)$  and  $\text{Var}(Z_K)$  are the mean and the variance of the asymptotic trace statistic provided by Larsson et. al. (1998)

- We employ the sequential procedure suggested by Johansen (1988)
- If one country has a higher rank than the hypothesed, the LR-bar statistic would asymptotically reject the null.
- Hence, this test gives the maximum cointegrating rank. [\[Go Back\]](#)

## PC-bar Test (Step 2)

$H_0$  : *cointegrating rank* $_i = r$  for all  $i = 1, \dots, N$

$H_1$  : *cointegrating rank* $_i < r$  for all  $i = 1, \dots, N$

- The PC-bar statistic converges to a standard normal as  $N$  and  $T \rightarrow \infty$ :

$$PC_r = \frac{\sqrt{N}[N^{-1} \sum_{i=1}^N \hat{c}_r^i - E(X_K)]}{\sqrt{Var(X_K)}} \Rightarrow N(0, 1)$$

where  $\hat{c}_r^i$  is the individual PC Harris statistic for unit  $i$  and  $E(X_K)$  and  $Var(X_K)$  are the mean and the variance of the variable  $X$  that has the same distribution as the asymptotic distribution of  $\hat{c}_r^i$

- This panel test is based on the principal component analysis of cointegrated time series of Harris (1997).
- If (at least) one of the individual ranks is less than the hypothesed, the test asymptotically rejects the null. [\[Go Back\]](#)

## Estimation Method in More Detail

- Considering  $y_{it}$  as the output for country  $i$  in year  $t$  and  $x_{it} = (\text{physical capital}_{it}, \text{human capital}_{it}, \text{infrastructure}_{it})$
- The equation to be estimated can be written as:

$$\begin{aligned}\Delta Y_i &= \phi_i \xi_i(\theta) + W_i \kappa_i + \varepsilon_i \quad i = 1, 2, \dots, N \\ \xi_i(\theta) &= Y_{i,-1} - X_{i,-1} \theta \quad i = 1, 2, \dots, N.\end{aligned}$$

where  $Y_i = (y_{i1}, \dots, y_{iT})'$ ,  $\xi_i(\theta)$  is the error correction component,  $W_i = (\Delta Y_{i,-1}, \dots, \Delta Y_{i,-p+1}, \Delta X_{i,-1}, \dots, \Delta X_{i,-p+1}, \iota)$  and  $\kappa_i = (\lambda_{i1}, \dots, \lambda_{i,p-1}, \delta'_{i1}, \dots, \delta'_{i,p-1}, \mu_i)'$ .

- Because the parameters of interest are the long-run effects, we work directly with the concentrated log-likelihood function.
- Moreover, once the pooled MLE of the long-run parameters is computed, the short-run and the error-correction coefficients can be consistently estimated by running the individual OLS regressions of  $\Delta Y_i$  on  $(\xi_i(\hat{\theta}), W_i)$  [\[Go Back\]](#)

# Alternative Explanatory Variables

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Table: Additional Results

Column	(1)	(2)	(3)	(4)	(5)
Variable Changed	Base	Total Phone Lines	Roads plus Rails	Paved Roads	BC Physical Capital
<b>Physical Capital</b>	<b>0.34</b>	<b>0.35</b>	<b>0.34</b>	<b>0.34</b>	<b>0.33</b>
t-ratio	35.2	32.8	35.2	26.6	18.0
hausman p-value	0.54	0.80	0.48	0.58	0.05
<b>Secondary Education</b>	<b>0.10</b>	<b>0.07</b>	<b>0.10</b>	<b>0.05</b>	<b>0.10</b>
t-ratio	15.6	6.84	15.8	3.98	10.3
hausman p-value	0.24	0.55	0.24	0.11	0.20
<b>Infrastructure</b>	<b>0.08</b>	<b>0.07</b>	<b>0.08</b>	<b>0.07</b>	<b>0.09</b>
t-ratio	7.45	5.45	7.51	5.20	5.53
hausman p-value	0.21	0.37	0.23	0.41	0.14
joint hausman p-value	0.44	0.69	0.43	0.33	0.20
Average R <sup>2</sup>	0.36	0.37	0.36	0.35	0.35

# Additional Homogeneity Tests

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Table: Homogeneity Tests

Column	(1)	(2)	(3)	(4)
	Per Capita Income (A)	Per Capita Income (B)	Infrastructure Endowment	Total Population
High	0.054	0.044	0.059	-0.016
Low	0.059	0.062	0.055	0.131
p-value	0.985	0.940	0.988	0.576